University of Science and Technology of		Academic year: 2025–2026	
Hanoi		Date: 07/10/2024 Time: 45 minutes Important instructions	
***		(according to lecturer's decision)	
Mid-term		1. No documents or communication devices are allowed.	
Subject: Algorithms and Data Structures		2. Copying or using Internet will lead to heavy penalty	
Sheet: 02 No of pages: 01			
Pathway coordinator		Lecturer (or Head of Subject)	Dr. Đoàn Nhật Quang
Student name		Student's ID	

Question 1 (16 pts)

A Harshad number is an integer that is divisible by the sum of its digits. Example:

- 18/(1+8) = 18/9 = 2, 18 is divisible by $2 \rightarrow$ Harshad number.
- 21/(2+1) = 21/3 = 7, divisible \rightarrow Harshad number.
- 19/(1+9) = 19/10 = 1.919, not divisible \rightarrow not a Harshad number.
- 274/(2+7+4) = 274/13 = 21.07, not divisible \rightarrow not a Harshad number.
- Implement a program in C/C++ using **Iteration** to find all Harshad numbers from 1 to n (n is a natural number). (7pts)
- Implement another **function using Recursion** to complete the above question. (7pts)
- Calculate the complexity of your functions or algorithms. Justify the answer (*comment directly in your source files*). (2pts)

Question 2 (4 pts)

Note: The student can answer this question in a text format. The submitted file can be either .c or .text.

A chat app buffers incoming messages to be displayed in the order they arrive.

- Propose an appropriate **data structure** to handle this display task. Justify your choice. (2pts)
- What are the basic functions to manipulate the proposed data structure? (1pt)
- Calculate the complexity of the display process. (1pt)