Data Mining - Classification I

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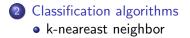
Classification

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- Context
- Overfitting



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Context Overfitting

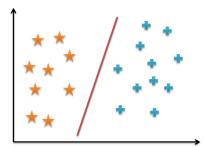
Classification vs Clustering

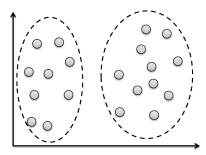
Classification

- Labeled data objects
- Assign a label to new objects

Clustering

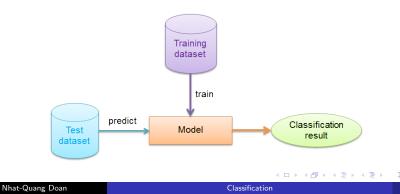
- Data is not labeled
- Identify structure in data and group objects





Objectives

- Classification is the supervised learning task of data mining that predicts categorical class labels (discrete or nominal)
- A model is built based on the training set and the class labels. This model helps in classifying new data



Applications

• Banking: card fraud detection



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Applications

• Pattern Recognition: Plate Recognition, Optimal Character Recognition





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Applications

• Security: Finger Print, Spam Filter.





Applications

• Transport: Self-driving vehicules.



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Problematics

Difficulties

- Training datasets: overfitting, imbalance of data, ...
- Information about data class
- Classification algorithms: complexity, training time, etc...
- Big data
- Performance

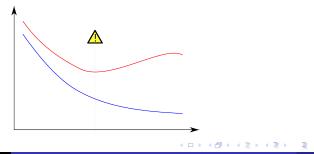
Input set: $(\mathcal{X}, \mathcal{Y}) = \{(\mathbf{x}_i, y_i)\}, \forall i = 1, ..., n: a set of n training objects$ $Object: <math>\mathbf{x}_i \in \mathbb{R}^d$ with $\mathbf{x}_i = (x_{i,1}, x_{i,2}, ..., x_{i,d}), y_i \in \mathcal{Y}$ (y_i is the class label of \mathbf{x}_i Model: Model \mathcal{M} allows to classify \mathcal{X} into many groups according to its \mathcal{Y} . Problem: For new object (test data) $\mathbf{x}_0 \notin \mathcal{X}$ and unknown y_0 , the model \mathcal{M} is employed to predict y_0 .

Overfitting

Definition

In data mining, overfitting problem occurs:

- A model is excessively complex, such as having too many parameters relative to the number of training objects.
- A model has poor predictive performance, as it overreacts due to the training data.



Overfitting

Overfitting

Many approaches to manage training datasets have been proposed to reduce variance and avoid overfitting:

- cross validation: leave-p-out , k-fold cross-validation
- bagging or bootstrap agrgregating
- and many more....

Training dataset generation

Cross-validation

This technique is a statistics model:

- generalize to an independent data set
- involve partitioning a sample of data into complementary subsets: building the model from one subset (the training set), and validating the model on the other subset (the testing set)

Context Overfitting

Training dataset generation

k-fold cross validation

- generalize to k subsets
- k-1 subsets for training and 1 subset for testing



5-fold cross validation

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Context Overfitting

Training dataset generation

Leave-p-out

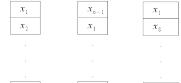
- Leave-p-out take p data out from the input dataset of n data, n - p for training and p for testing
- This cross-validation requires to learn and validate C_n^p times (if n = 100 and p = 30, $C_{100}^{30} = 3 * 10^{25}$)
- Leave-one-out is often used as for $C_n^1 = n$

Context Overfitting

Training dataset generation

Bagging

- consider input set X with n training objects
- create k new training sets X_i by drawing n objects with replacement



	x_{n-2}		x_{n-1}		<i>x</i> _n	
	x_{n-1}		<i>x</i> ₁₀		x_n	
n	x_n		<i>x</i> ₄		<i>x</i> ₂	
	X		X _{bootstrap}		X _{bootstrap}	

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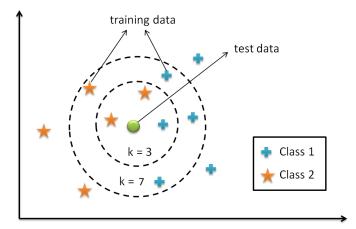
Definition

k-NN

k-Nearest Neighbors algorithm (or k-NN for short) is a non-parametric method often used for classification.

- The input consists of the k closest training examples in the feature space.
- The output is a class label. An object is classified by a majority vote of its neighbors, with the object being assigned to the class most common among its k nearest neighbors.
- k is a positive integer, typically small for example k = 1, 3, 5, 10, etc.





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Pros and Cons

Advantages

- No input parametric
- No training step required
- Simple to understand and to interpret

Disadvantages

- Require many operations for testing
- Low accuracy comparing to Decision Tree, Random Forest, SVM, Neural Networks, etc...

Binary Classification

Input set: $(\mathcal{X}, \mathcal{Y}) = \{(\mathbf{x}_i, y_i)\}, \forall i = 1, ..., n: a set of N training objects$ $Object: <math>\mathbf{x}_i \in \mathbb{R}^d$ with $\mathbf{x}_i = (x_{i,1}, x_{i,2}, ..., x_{i,d}), y_i \in \mathcal{Y}$ (y_i is $\{-1; +1\}$ Model: A learn classifier $f(\mathbf{x}_i)$ such that

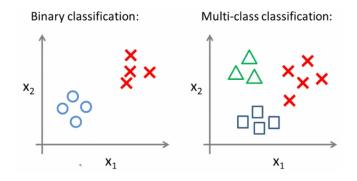
$$f(\mathbf{x}_i) = \begin{cases} \geq 0 & y_i = +1 \\ < 0 & y_i = -1 \end{cases}$$

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k-neareast neighbor

Binary Classification

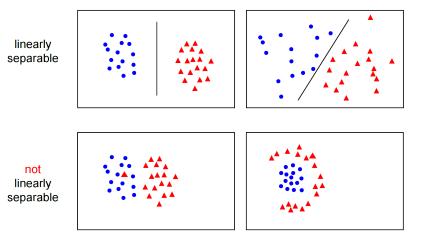


Binary vs Multi-class classification

A multi-class classifier is able to classify into more 2 classes. Binary classifier can only deal with 2-class problems

k-neareast neighbor

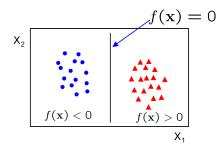
Binary Classification



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Binary Classification



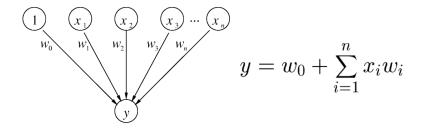
A linear classifier has the form:

$$f(\mathbf{x}) = \mathbf{w}\mathbf{x}^T + b$$

- in 2D the discriminant is a line, in kD (k ≥ 3), is a hyperplane denoted by Δ(v, a) = {x ∈ ℝ^d |vx^T + a = 0}
- w is the normal to the line, and b the bias
- w is known as the weight vector

Perceptron

- An algorithm for supervised learning of binary classifiers.
- A type of linear classifier.



Given linearly separable data \mathcal{X} labelled into two categories $y_i = \{-1, 1\}$, find a weight vector **w** such that the discriminant function:

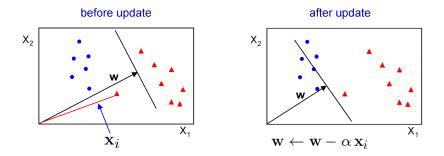
$$f(\mathbf{x}) = \mathbf{w}\mathbf{x}^T$$

Perceptron Algorithm

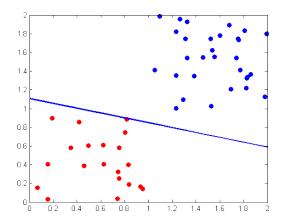
- intialize $\mathbf{w}_0 = \mathbf{0}$ (or close to $\mathbf{0}$)
- for all $\mathbf{x}_i \in \mathcal{X}$, if \mathbf{x}_i is misclassified

$$\mathbf{w}_t = \mathbf{w}_{t-1} + \alpha \operatorname{sign}(f(\mathbf{x}_i))\mathbf{x}_i$$

• until all the data is correctly classified



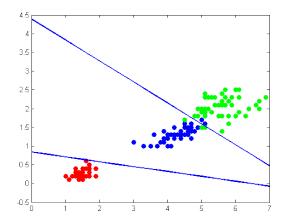
if the data is linearly separable, then the algorithm will converge. After the convergence, $\mathbf{w} = \alpha \sum \mathbf{x}_i$.



Perceptron Classifier for 2-class dataset

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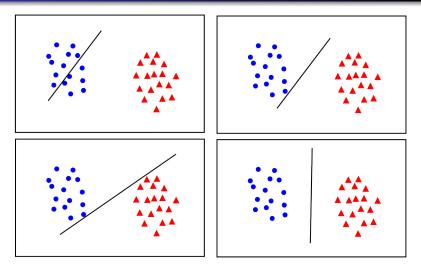
- Convergence can be slow and Perceptron algorithm depends heavily on input parameters ${\bf w}_0$ and α
- Perceptron is able to handle 2-class problems.
- How to use Perceptron for multi-class problems?
- What if we have 3 classes such as Iris dataset?



Perceptron Classifier for Iris dataset

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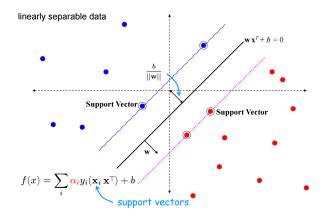
Binary Classification



Are all decision boundaries equally good? or what is the best $\boldsymbol{w}?$

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The decision boundary or the hyperplan should be as far away from the data of both classes as possible.



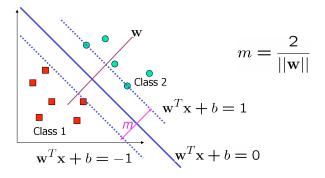
A support vector machine (SVM) is a supervised learning technique from the field of machine learning applicable to both classification and regression.

- Rooted in the Statistical Learning Theory developed by Vladimir Vapnik and co-workers at AT&T Bell Laboratories in 1995
- Very famous due to its success for hand writting recognitions (or image classification in general)

- SVMs are based on the principle of Structural Risk Minimization.
- Non-linearly map the input space into a very high dimensional feature space in order to construct an optimal separating hyperplane in this space (a maximal margin classifier)

The margin, the smallest distance between the decision boundary $\Delta(\mathbf{v}, a)$ and the examples \mathbf{x}_i , must be maximized.

$$m = min_{i=1..n} dist(\mathbf{x}_i, \Delta(\mathbf{v}, a))$$



Let **x** be a vector in \mathbb{R}^d and $\Delta(\mathbf{v}, a) = \{\mathbf{s} \in \mathbb{R}^d | \mathbf{v}\mathbf{s}^T + a = 0\}$ an hyperplane. The distance between **x** and the hyperplan $\Delta(\mathbf{v}, a)$ is

$$\mathit{dist}(\mathbf{x},\Delta(\mathbf{v},a)) = rac{|\mathbf{v}\mathbf{x}^T+a|}{||v||}$$

Let \boldsymbol{s}_{x} be the closest point to $\boldsymbol{x} \in \Delta, \boldsymbol{s}_{x} = \textit{argmin}||\boldsymbol{x} - \boldsymbol{s}||,$

$$\mathbf{x} = \mathbf{s}_{x} + m \frac{\mathbf{v}}{||\mathbf{v}||} \iff \mathbf{x} - \mathbf{s}_{x} = m \frac{\mathbf{v}}{||\mathbf{v}||}$$

So that, taking the scalar product with vector \mathbf{v} we have:

$$\mathbf{v} \times m \frac{\mathbf{v}^T}{\mathbf{v}} = \mathbf{v}(\mathbf{x}^T - \mathbf{s}_x^T) = \mathbf{v}\mathbf{x}^T - \mathbf{v}\mathbf{s}_x^T = \mathbf{v}\mathbf{x}^T + a - (\mathbf{v}\mathbf{s}_x^T + a) = \mathbf{v}\mathbf{x}^T + a$$

$$\mathbf{vs}_x^T + a = 0$$
 because $\mathbf{s}_x \in \Delta$

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So, therefore

$$\mathbf{v} \times m \frac{\mathbf{v}^T}{||\mathbf{v}||} = m \frac{||\mathbf{v}||^2}{||\mathbf{v}||} = m||\mathbf{v}|| = \mathbf{v}\mathbf{x}^T + \mathbf{a}$$

Thus,

$$m = \frac{\mathbf{v}\mathbf{x}^T + \mathbf{a}}{||\mathbf{v}||}$$

 and

$$\textit{dist}(\mathtt{x}, \Delta(\mathtt{v}, a)) = rac{|\mathtt{v} \mathtt{x}^{ op} + a|}{||v||}$$

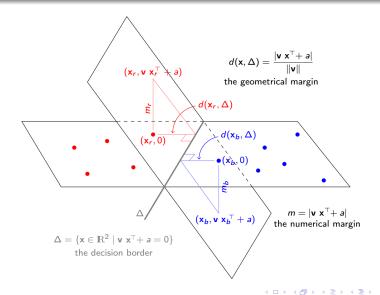
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Introduction Classification algorithms

k-neareast neighbor

Support Vector Machines



The decision hyperplane $\Delta(\mathbf{v}, a) = {\mathbf{s} \in \mathbb{R}^d | \mathbf{vs}^T + a = 0}$, we have to maximize the margin

$$\max_{\mathbf{v},a} \min_{i \in [1..n]} dist(\mathbf{x}_i, \Delta(\mathbf{v}, a))$$

Maximize the confidence

$$\begin{cases} \max_{\mathbf{v},a} m & \qquad \\ \text{with } \min_{i \in [1..n]} \frac{|\mathbf{v}\mathbf{x}^T + a|}{||v||} \ge m & \qquad \\ \text{with } \frac{y_i(\mathbf{v}\mathbf{x}^T + a)}{||v||} \ge m \end{cases}$$

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Change variable $\mathbf{w} = \frac{\mathbf{v}}{m||\mathbf{v}||} \implies ||\mathbf{w}|| = \frac{1}{m}$ and $b = \frac{a}{m||\mathbf{v}||}$ Maximize the confidence

$$\max_{\mathbf{v},a} m$$
 with $\frac{y_i(\mathbf{vx}^T+a)}{||v||} \ge m$

$$\begin{cases} \max_{\mathbf{w},b} m \\ \text{with } y_i(\mathbf{w}\mathbf{x}^T + b) \ge 1; i = 1..n \\ \text{and } m = \frac{1}{||\mathbf{w}||} \end{cases} \begin{cases} \min_{\mathbf{w},a} ||\mathbf{w}|| \\ \text{with } y_i(\mathbf{w}\mathbf{x}^T + b) \ge 1; i = 1..n \end{cases}$$

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Linear SVMs are the solution of the following problem (called primal)

Let $\{(\mathbf{x}_i, y_i); i = 1..n\}$ be a set of labelled data with $\mathbf{x} \in \mathbb{R}^d, y_i \in \{1, -1\}$. A support vector machine is a linear classifier associated with the following decision function: $D(x) = sign(\mathbf{wx}^T + b)$ where $\mathbf{w} \in \mathbb{R}^d$ and $b \in \mathbb{R}$ a given thought the solution of the following problem:

$$\begin{cases} \min_{\mathbf{w}\in\mathbf{R}^{d},b\in\mathbb{R}} & \frac{1}{2}||\mathbf{w}||^{2} \\ \text{with} & y_{i}(\mathbf{w}\mathbf{x}^{T}+b) \geq 1; i = 1..n \end{cases}$$

Minimize
$$\frac{1}{2}||\mathbf{w}||$$

subject to $1 - y_i(\mathbf{wx}^T + b) \le 0$ for $i = 1..n$
The Lagrangian is:

$$\mathcal{L} = \frac{1}{2} \mathbf{w} \mathbf{w}^{T} + \sum_{i=1}^{n} \alpha_{i} (1 - y_{i} (\mathbf{w} \mathbf{x}^{T} + b))$$

Note that $||\mathbf{w}|| = \mathbf{w}\mathbf{w}^T$ and $\alpha_I \ge 0$

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$$\mathcal{L} = \frac{1}{2} \mathbf{w} \mathbf{w}^{T} + \sum_{i=1}^{n} \alpha_{i} (1 - y_{i} (\mathbf{w} \mathbf{x}^{T} + b))$$

Setting the gradient of ${\mathcal L}$ w.r.t. ${\boldsymbol w}$ and ${\boldsymbol b}$ to zero, we have:

 $\frac{\delta \mathcal{L}}{\delta \mathbf{w}} =$

$$\frac{\delta \mathcal{L}}{\delta b} =$$

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If we substitue $\mathbf{w} = \sum_{i=1}^{n} \alpha_i y_i \mathbf{x}_i$ to \mathcal{L} , we have

$$\mathcal{L} = \sum_{i=1}^{n} \alpha_i - \frac{1}{2} \sum_{i=1}^{n} \sum_{j=1}^{n} \alpha_i \alpha_j y_i y_j \mathbf{x}_i \mathbf{x}_j^T$$

- Note that $\sum_{i=1}^{n} \alpha_i y_i = 0$
- This is a function of α
- It is known as the dual problem: if we know w, we know all α; or if we know all α, we know w

Thue dual problem is thus:

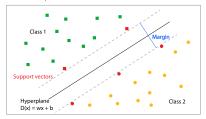
$$\max \sum_{i=1}^{n} \alpha_{i} - \frac{1}{2} \sum_{i=1}^{n} \sum_{j=1}^{n} \alpha_{i} \alpha_{j} y_{i} y_{j} \mathbf{x}_{i} \mathbf{x}_{j}^{T}$$

subject to $\alpha_i \geq 0$ and $\sum_{i=1}^n \alpha_i y_i = 0$

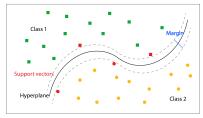
- \mathbf{x}_i with non-zero α_i are called support vectors (SV)
- w = Σⁿ_{i=1} α_iy_ix_i is linear combination of a small number of data points
- To test new data z
 - compute $\mathbf{w}\mathbf{z}^{T} + b = \sum_{j=1}^{s} \alpha_{j} y_{j}(\mathbf{x}_{j}\mathbf{z}^{T}) + b$
 - if the sum is positive, **z** is classified as class 1 or class 2 otherwise.

• Up to now, we have only seen large-margin classifier with a linear decision boundary. How to do if our problem is nonlinear?

Linear separation







• To handle non-linearly separable problems, we use error ξ

$$\begin{cases} \mathbf{w}^{\mathsf{T}} \mathbf{x}_i + b \ge 1 - \xi_i & y_i = 1 \\ \mathbf{w}^{\mathsf{T}} \mathbf{x}_i + b \le -1 + \xi_i & y_i = -1 \\ \xi_i \ge 0 & \forall i \end{cases}$$

 ξ_i are slack variables in optimization, ξ = 0 if there is no error for x_i

We want to minimize

$$\frac{1}{2}||\mathbf{w}||^2 + C\sum_{i=1}^n \xi_i$$

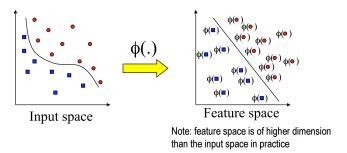
• The dual of this new problem is:

$$\max\sum_{i=1}^{n} \alpha_{i} - \frac{1}{2}\sum_{i=1}^{n}\sum_{j=1}^{n} \alpha_{i}\alpha_{j}y_{i}y_{j}\mathbf{x}_{i}\mathbf{x}_{j}^{T}$$

subject to $C \ge \alpha_i \ge 0, \sum_{i=1}^n \alpha_i y_i = 0$

• This is similar to the problem in the linear separable case.

- Up to now, we have only seen large-margin classifier with a linear decision boundary. How to do if our problem is nonlinear?
- Idea: transform x_i to a higher dimensional space to "make life easier"



- Computation in the feature space is costly because it is high dimensional
- Kernel functions are used to overcome this.

• The dual of this new problem is:

$$\max \sum_{i=1}^{n} \alpha_{i} - \frac{1}{2} \sum_{i=1}^{n} \sum_{j=1}^{n} \alpha_{i} \alpha_{j} y_{i} y_{j} \mathbf{x}_{i} \mathbf{x}_{j}^{\mathsf{T}}$$

subject to $C \ge \alpha_i \ge 0, \sum_{i=1}^n \alpha_i y_i = 0$

- We just calculate the inner product without explicite the mapping of original data to the feature space.
- Geometric similarity measures can be expressed by inner products.
- Kernal function is often defined as:

$$K(\mathbf{x}_i, \mathbf{x}_j) = \phi(\mathbf{x}_i)\phi(\mathbf{x}_j)^T$$

Examples of kernel functions

• Linear kernels

$$K(\mathbf{x}, \mathbf{y}) = \mathbf{x}\mathbf{y}^T$$

• Polynomial kernels with degree d

$$K(\mathbf{x},\mathbf{y}) = (\mathbf{x}\mathbf{y}^{\mathcal{T}}+1)^d$$

Gaussian kernels

$$K(\mathbf{x},\mathbf{y})=e^{rac{-||\mathbf{x}-\mathbf{y}||^2}{2\sigma^2}}$$

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Special transformation from $\mathbb{R}^2 \to \mathbb{R}^3$

$$\phi(\mathbf{x}) = \phi : (x_1, x_2) \to (x_1^2, x_2^2, \sqrt{2}x_1x_2)$$
$$\phi(\mathbf{x})\phi(\mathbf{y})^T = (\mathbf{x}\mathbf{y}^T)^2$$

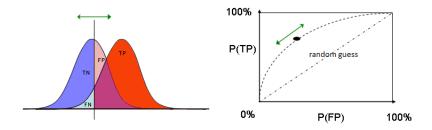
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Evaluation

Confusion Matrix Prediction outcome Positive Negative total $Precision = \frac{TP}{P}$ False True P' Positive Actual Positive Negative value $Recall = \frac{TP}{P'}$ $Accuracy = \frac{TP + TN}{P + N}$ True False Negative N′ Positive Negative Ρ Ν total

Introduction Classification algorithms

Evaluation

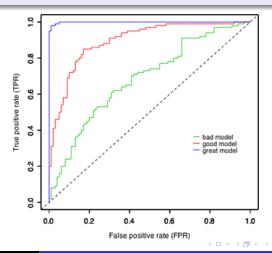


A receiver operating characteristic (ROC), or ROC curve, is a graphical plot that illustrates the performance of a binary classifier system.

- True positive rate (TPR) vs False positive rate (FPR) at various threshold settings.
- Cost vs benefit analysis of decision making.

Evaluation

To compare different binary classifiers, AUC (Area under ROC curve) becomes a good criterion.



Nhat-Quang Doan

Classification

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