Data Structures II - Stacks & Queues

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Linked Lists

Linear Data Structures:

- Lists
 - Definition: is a collection with a finite number of data objects (same type) and has a finite size.
 - List data structure: Array-based Lists, Linked Lists
 - List Operations
- Stacks
- Queues

Today Objectives

- Introduce the basics of Stacks and Queues: declaration, initialization, and use.
- Learn different functions and operations with Stacks and Queues: add, remove, search, etc.
- Implement examples in C/C++.

Plan

Stacks

Queues



Stack of books



Stack of coins

General Definition

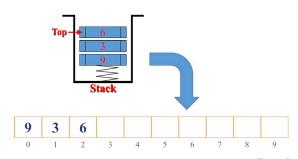
A **stack** is a pile of objects, typically one that is neatly arranged.

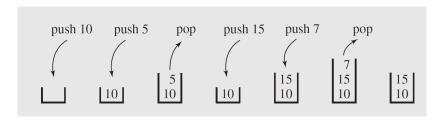
Programming Definition

A **stack** is a container of objects inserted and removed according to the First In Last Out (FILO) principle.

Principle

- A linear data structure is used to store data in a particular order.
- Storing and retrieving data are performed only on the top: Push inserts an element; Pop removes the last element that was added.
- Access of items in a stack is restricted; it follows First In Last Out (FILO) order.





Push and pop operations follow FILO order.

Stack Application

- Expression evaluation: calculate arithmetic expression.
- Backtracking: This is a process when you need to access the most recent data element in a series of elements
 - Find your way through a maze.
 - Find a path from one point in a graph (roadmap) to another point.
 - Play a game with moves to be made (checkers, chess, sudoku).
- Undo/Redo-mechanism of text editors (Back/Forward Navigation of web-browsers).
- Call stack in recursive functions.
- Data structures for Machine Learning algorithms.



Stack Application

Arithmetic Expression:

• infix - operation between operands

$$(3+5)*10$$

• prefix - operation before operands

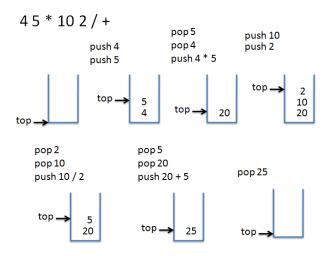
• postfix - operation after operands

Stack Application

Arithmetic Expression: evaluating postfix

- repeat
 - find the first operation preceded by two operands
 - evaluate and replace
- Example:

= 25



Stacks implementation may offer the possible operations:

- init(): create an empty stack.
- isEmpty(): check if the stack is empty.
- push(): add a new item at the top of a stack.
- pop(): remove the top item of a stack.
- top(): retrieve the top item of a stack.

Other operations can be possibly defined:

- size(): return the size of a stack.
- isFull(): check if the stack is full.
- display(): display the content of a stack.
- etc.

Stack Data Structure

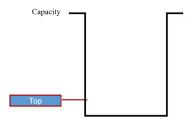
There are several solutions to the stack implementation using different declarations.

- Static array-based stack: arrays can be simply used to manipulate collections of items.
- Dynamic array-based stack: malloc() is capable of representing a stack.
- Linked stack: A very flexible mechanism for dynamic memory management is provided by pointers.

The idea is to store a stack in a fixed-size static array for simple implementation.

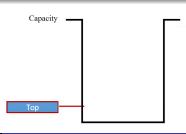
```
• init(): this function allows for creating an empty stack.

1 void init(Stack *st) {
2    // st must get malloc() in main()
3    st->top = -1;
4 }
```



 init(): this alternative function allows for creating an empty stack.

```
Stack * init(Stack *st) {
   st = (Stack*)malloc(sizeof(Stack));
   st->top = -1;
   return st;
}
```



return st.top+1;

```
• isEmpty(): this action allows checking if a stack is empty.

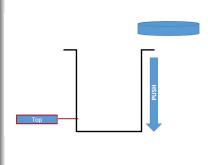
int isEmpty(Stack st){
  return (st.top < 0);
}

• size(): this function returns the stack size.

int size(Stack st){</pre>
```

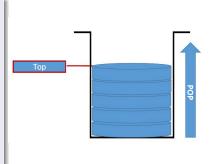
• push(): this function allows to add a new item into a stack.

```
1  void push(Stack *s, int val){
2   if (isFull(*s))
3     printf(''Stack is full!'');
4   else{
5     s->top ++;
6     s->data[s->top] = val;
7   }
8 }
```



 pop(): this function allows to remove the top item from a stack,

```
void pop(Stack *s){
if (isEmpty(*s))
printf(''Stack empty!'');
else{
s->top --;
}
}
```



Dynamic Array-Based Stacks

The idea is to perform the stack implementation with a dynamic array.

```
1 struct _Stack {
2    int top;
3    int capacity
4    int *data;
5 };
6 typedef struct _Stack Stack;
```

Dynamic Array-Based Stacks

```
• init(): this function allows to create an empty stack.

1 void init (Stack *s, int N) {
    // s gets malloc() in the main() function
    s->top = 0;
    s->capacity = N;
    s->array = (int *) malloc(s->capacity);
}
```

Array-Based Stacks

Array-based stack implementation:

Pros

- Simple to understand and implement.
- Stack is asserted at the top without changing other elements.

Cons

• Stack size has to be manipulated.

Stack Implementation with Linked Lists

Definition

In this implementation, each item is placed together with the link to the next item, resulting in a simple component called a node:

- A data part stores an element value of the stack.
- A next part contains a link (or pointer) that indicates the node's location containing the next element.

Stack Implementation with Linked Lists

```
Implementing a stack as a linked list:

1    struct _Node{
        int data;
        struct _Node *next;

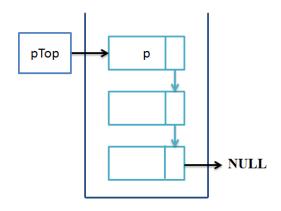
4    };

5    typedef struct _Node Node;

6    struct _Stack{
        int size;
        Node *pTop;

9    };

10    typedef struct _Stack Stack;
```



Stacks Implementation with Linked Lists

Several basic operations are re-written to adapt to the new use of stack implementation.

```
void init(Stack *s){
// s gets malloc() in the main() function
s->size = 0;
s->pTop = NULL;
}
int isEmpty(Stack st){
return (st.size);
}
```

Stack Implementation with Linked Lists

```
Push operation is adapted to the new declaration:
    int push(int newData, Stack *st){
       Node *pnew;
3
       pnew=(Node *) malloc(size of (Node));
       if (pnew == NULL)
5
         return 0:
6
       pnew->data = newData;
       //insert at the beginning of the list
8
       pnew->next = st->pTop->next;
9
       st->pTop = pnew;
10
       st \rightarrow size ++:
11
       return 1:
12
```

Stack Implementation with Linked Lists

```
Pop operation is adapted to the new declaration:
   int pop(stack *st){
       Node *p;
       if (isEmpty(*st))
          return 0; // fail to pop
5
       p = st - pTop;
6
       st->pTop = st->pTop->next;
       st->size--:
       free(p);
       return 1:
10
```

Complexity

Comparisons of complexity for different stack implementations

	push()	pop()	top()
Array-based Stacks	O(1)	O(1)	O(1)
Stacks with Linked List	O(1)	O(1)	O(1)

Stack Implementation with Linked Lists

Pros

• Stack implementation with linked lists is flexible to the size and memory.

Cons

• If the top element is not used in the implementation, we have to traverse all the elements in the stack to find the top.



General Definition

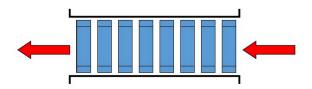
A **queue** is a line or sequence of people or vehicles awaiting their turn to be attended to or to proceed.

Programming Definition

A **queue** is a container of objects (a linear collection) that are inserted and removed according to the first-in-first-out (FIFO) principle.

Principle

- A special data structure of lists used to store data in a particular order.
- Basic operations are done in both ends: insert at one end (back/rear) and remove at the other end (front/head).
- Access of items in a Queue is restricted; it follows the First In First Out (FIFO) order.



Queue Application

Typical uses of queues are in simulations and operating systems.

- Operating systems often maintain a queue of processes ready to execute or to wait for a particular event to occur.
- Anything that involves "waiting in line": printing on the computer, seating customers at a restaurant, etc.

Queues are an abstract data structure, and its implementation may offer the possible operations:

- init(): initialize an empty queue.
- isEmpty(): check if the queue is empty.
- enqueue(): add a new item at the back of the queue.
- dequeue(): remove the front item of the queue.

Other operations can be possibly defined:

- length(): return the size of a queue.
- front(): retrieve the front item of the queue.
- isFull(): check if the queue is full.
- display(): display the content of a queue.

Queues

Queues

There are several solutions to queue implementation using different declarations.

- Static array-based queue: arrays can be simply used to manipulate collections of items.
- Dynamic array-based queue: **malloc()** is capable of representing a queue.
- Linked queue: A very flexible mechanism for dynamic memory management is provided by pointers.

The idea is to store a queue in a fixed-size static array for simple implementation.

```
1 struct _Queue {
2    int data[CAPACITY];
3    int front, back;
4    // front is optional
5 };
6 typedef struct _Queue Queue;
```

• init(): this function allows to create an empty queue.

void init(Queue *q){
 // q gets malloc() in the main() function
 q->front = 0;
 q->back = 0;
}

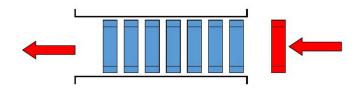
• isEmpty(): this operation verifies that a queue is empty.

```
int isEmpty(Queue *q){
return (q—>back ==0);
}
```

```
• length(): this operation returns the queue size.

1 int length(Queue *q){
2   int l = q->back-q->front;
3   return l;
4 }
```

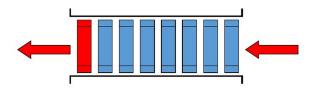
Due to the FIFO order, new items are inserted at the back of the queue. The function enqueue() allows to add a new item into a queue.



There are three cases to be proceeded for enqueue(): the queue is full, empty, and has at least one item.

```
int enqueue(Queue *q, <DataType> newData){
       if (length(q) = CAPACITY){
3
           printf("Queue-is-full!");
           return 0:
5
6
          (isEmpty(q)){
           q \rightarrow val[0] = newData;
8
       } else {
              int idx = q->back;
10
              q\rightarrow val[idx] = newData;
11
12
       q->back++:
13
       return 1;
14
```

Due to the FIFO order, if we want to remove items from a queue, this action will proceed at the front of the queue. The function dequeue() asserts the deletion.



Two possible cases for dequeue() must be manipulated: when the queue is empty or not empty.

```
int dequeue(Queue *q){
        if (isEmpty(q))
3
           return 0;
4
        else {
5
           if (length(q) > 1){
6
               for (int i = 1; i < length(q); i++)
                   q\rightarrow val[i-1] = q\rightarrow val[i];
8
9
           q->back = q->back-1;
10
11
       return 1:
12
```

Dynamic Array-Based Queues

A dynamic array-based Queue improves the static array-based implementation.

```
1 struct _Queue{
2    int front, back;
3    int capacity;
4    int *val;
5    };
6 typedef struct _Queue Queue;
```

Dynamic Array-Based Queues

```
init(): this function allows to create an empty queue.

void init(Queue *q, int N){
    // q gets malloc() in the main() function
    q->back = 0;
    q->front = 0;
    q->capacity = N;
    q->val = (int *) malloc(q->capacity);
}
```

Array-Based Queues

Array-based queue implementation:

Pros

- Simple to understand and implement.
- Enqueue is asserted at the back without shifting elements.

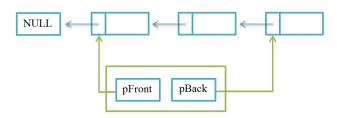
Cons

- Only the first element is accessible.
- All the elements have to be shifted (O(n) time for a queue with n elements) after a dequeue.

Definition

In this implementation, each item is placed together with the link to the next item, resulting in a simple component called a node:

- A data part stores an element value of the queue.
- A next part contains a link (or pointer) that indicates the node's location containing the next element.
- The front element points to NULL.



Queue implementation using a linked list

```
1 typedef struct _Node {
2    int data;
3    struct _Node *next;
4 } Node;
5 typedef struct _Queue {
6    Node *pFront, *pBack;
7    int size;
8 }Queue;
```

Several basic operations are re-written to adapt to the new use of queue implementation.

```
void init(Queue *q){
    // q gets malloc() in the main() function

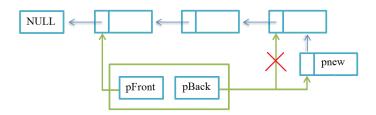
q->size = 0;

q->pFront = q->pBack = NULL;

int isEmpty(Queue q){
    return (q->qFront == NULL);
}
```

Enqueue operation:

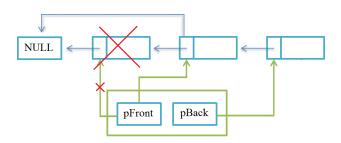
- New items are enqueued at the back of the queue.
- The back node points to new items.



```
void enqueue (Queue *q, int _val){
      Node *pnew = (Node *) malloc(sizeof(Node));
3
      pnew—>val = _val;
4
      pnew->next = NULL;
5
       if (q->pFront == NULL)
6
          q\rightarrow pFront = q\rightarrow pBack = pnew;
      else{
8
          pnew->next = q->pBack;
9
          q-pBack = pnew;
10
11
      q \rightarrow size++:
12
```

Dequeue operation:

- The list should have at least one element.
- The front node points to the node that points to the first one.
- The pointer of this node points to NULL.



```
void dequeue(Queue *q){
    if (isEmpty(*q))
 3
            return 0:
4
        else {
5
            if (q\rightarrow size = 1){
                q->pFront = q->pBack = NULL;
6
                q\rightarrow size --:
8
9
            else{
10
                Node *p = q->pBack;
11
                while (p\rightarrow next != q\rightarrow pFront)
12
                        p = p->next;
13
                q->pFront = p;
                q->pFront->next = NULL;
14
15
                q\rightarrow size --:
16
17
18
        return 1:
19
```

Complexity

Comparisons of complexity for different queue implementations

	enqueue()	dequeue()	front()
Array-based Queues	O(1)	O(n)	O(1)
Queues wLL (with pFront, pBack)	O(1)	O(n)	O(1)
Queues wLL (without pFront)	O(1)	O(n)	O(n)
Queues wDLL (with pFront, pBack)	O(1)	O(1)	O(1)

LL - Singly Linked List; DLL - Doubly Linked List

Pros

- Flexible to the size and memory.
- Enqueue can be done without shifting elements.

Cons

 Have to traverse all the way to find the second element for the dequeue