

Gather - Scatter

Tran Giang Son, tran-giang.son@usth.edu.vn

ICT Department, USTH

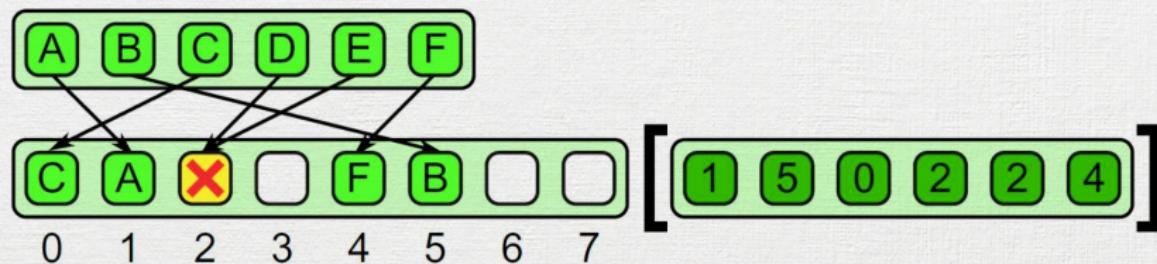


Scatter

What?

- “Sequential read, scattered random write”
- A relationship *from input to output*
- Smaller set of values is distributed (**written**) into another array
 - [Optional] with an index vector
- There may be gaps in the output array
- Highly memory intensive

What?



Why?

- Efficient memory access
 - Pre-cache contents
- Array of Struct (AoS) to Struct of Array (SoA)
- Building block of other algorithms
 - e.g. Radix sort

How?

- In below examples, lookup is a lookup index table
- In serial fashion

```
for i in range(N):  
    dst[lookup[i]] = src[i]
```

- In parallel

```
tidx = ...  
dst[lookup[tidx]] = src[tidx]
```

Examples

- RGB to HSL

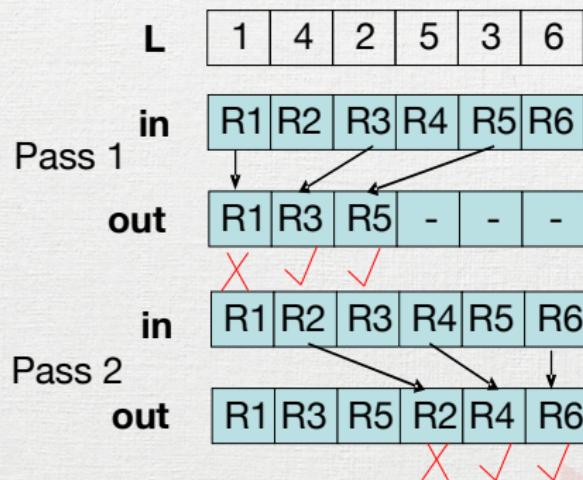
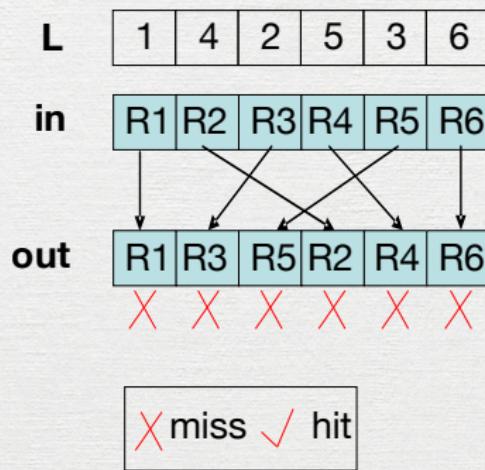
```
outH[tid] = h  
outS[tid] = s  
outL[tid] = l
```

Optimization

- Exploit cache locality
- Multi-pass scatter ¹
 - n passes
 - Divide output to n areas
 - In i^{th} pass
 - Check destination
 - Write only if in i^{th} area

¹Efficient Gather and Scatter Operations on Graphics Processors

Optimization



Labwork 8: Scatter

- To prepare for the next “Gather” labwork, we need to convert the input image:
 - From RGB to HSV, from AoS to SoA: to 3 different arrays ($H[]$, $S[]$, $V[]$)
 - Reversely, from HSV to RGB, from SoA to AoS
- Implement the two scatter 2D kernels `RGB2HSV()` and `HSV2RGB()`
- Test the two kernels for a sample image (convert to HSV and convert back to RGB), compare the output with the input image
- Write a report (in `LATEX`)
 - Name it « Report.8.scatter.tex »
 - Explain how you implement the labworks

Extra: HSV

- Hue, Saturation, Value
 - $H \in [0..360]$: “The color”. Red? Yellow? Cyan? Magenta?
 - $S \in [0..1]$: “The colorfulness”. Really cyan? Light yellow?
 - $V \in [0..1]$: “The brightness”. Dark cyan? Crimson?

Extra: RGB to HSV

- Preparation

- Scale R, G, B to $[0..255]$ to $[0..1]$
- Find \max and \min among $R, G, B \in [0..1]$
- $\Delta = \max - \min$

- Conversion

$$H = \begin{cases} 0^\circ & \Delta = 0 \\ 60^\circ \times \left(\frac{G-B}{\Delta} \bmod 6 \right) & \max = R \\ 60^\circ \times \left(\frac{B-R}{\Delta} + 2 \right) & \max = G \\ 60^\circ \times \left(\frac{R-G}{\Delta} + 4 \right) & \max = B \end{cases}$$

$$S = \begin{cases} 0 & \max = 0 \\ \frac{\Delta}{\max} & \max \neq 0 \end{cases}$$

$$V = \max$$

Extra: HSV to RGB

- Preparation
- $d = H/60$
- $hi = (\text{int})d \bmod 6$
- $f = d - hi$
- Conversion
- $l = V \times (1 - S)$
- $m = V \times (1 - f \times S)$
- $n = V \times (1 - (1 - f) \times S)$

$$(R, G, B) = \begin{cases} (V, n, l) & 0^\circ \leq H < 60^\circ \\ (m, V, l) & 60^\circ \leq H < 120^\circ \\ (l, V, n) & 120^\circ \leq H < 180^\circ \\ (l, m, V) & 180^\circ \leq H < 240^\circ \\ (n, l, V) & 240^\circ \leq H < 300^\circ \\ (V, l, m) & 300^\circ \leq H < 360^\circ \end{cases}$$

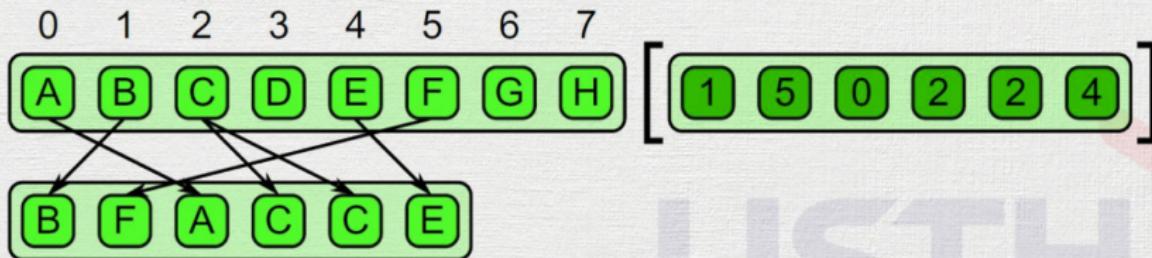
- Scale R, G, B from $[0..1]$ to $[0..255]$

Gather



What?

- “Gathered random read, sequential write”
- A relationship *from output to input*
- Large set of values are **read** from an array
 - [Optional] with an index vector
- No gap in the output array
- Highly memory intensive



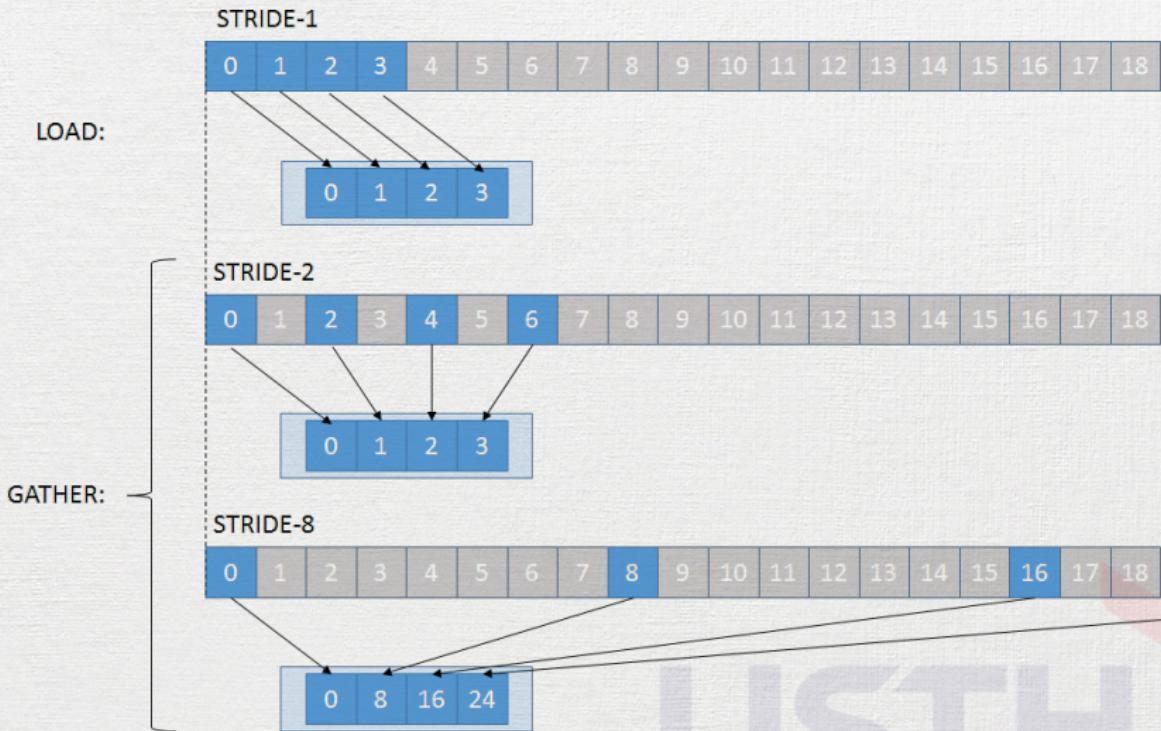
Why?

- Struct of Array (SoA) to Array of Struct (AoS)
 - Efficient memory access
- Building block of other algorithms
 - e.g. Radix sort

Why?

- Strided memory access
 - Memory fields accessed are equally distant
 - Called a stride
- Gathered \Rightarrow contiguous access

Why?



How?

- In below examples lookup is a lookup index table
- In serial fashion

```
for i in range(N):  
    dst[i] = src[lookup[i]]
```

- In parallel

```
tid = ...  
dst[tid] = src[lookup[tid]]
```

Example

- Horizontally flipping image

```
dst[tidy][tidx][0] = src[tidy][w - tidx][0]
```

```
dst[tidy][tidx][1] = src[tidy][w - tidx][1]
```

```
dst[tidy][tidx][2] = src[tidy][w - tidx][2]
```

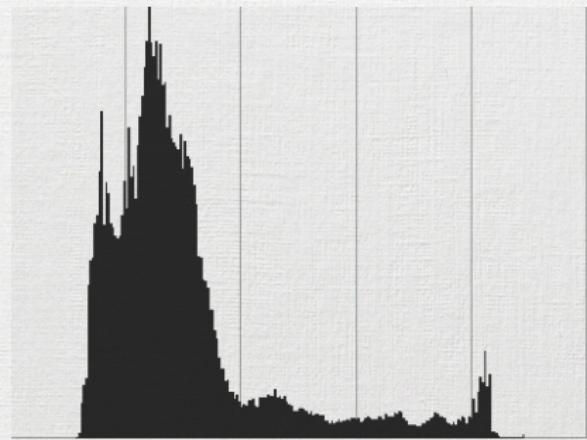
Labwork 9: Histogram Equalization

- Implement labwork 9a: Histogram
 - Calculate histogram of input **grayscale** image
- Implement labwork 9b: Histogram Equalization for **grayscale** image
 - Equalize the histogram for that input image
- Write a report (in L^AT_EX)
 - Name it « Report.9.gather.tex »
 - Explain how you implement the labworks
 - Explain and measure speedup, if you have performance optimizations
- Push the report and your code to your forked repository

Extra 9a: Histogram

- Graphical representation of the value distribution in a digital image
 - Divide range of values to certain ranges (“bins”)
 - Count number of value occurrences for each “bin”
- For image: an array, each element i in the array counts the number of pixels having gray level i

Extra 9a: Histogram



Extra 9a: Histogram

In serial

```
for y in range(height):
    for x in range(width):
        histo[input[y][x]]++
```

Extra 9a: Histogram

In parallel: 2 ways

- Atomic operations
 - Race condition due to parallelization
 - Not discussed this week. Next week with Prof. Lillian Aveneau.
- Local histogram
 - Each thread calculates a local histogram `lhisto[]` of a region in image (GATHER)
 - A sum is then combined for all regions (REDUCTION)

Extra 9b: Histogram Equalization

- Previously, grayscale stretch (LW 7)
 - Increases global contrast
 - Linearly calculates intensity of each pixel from $[min..max]$ to $[0..255]$
- Histogram equalization
 - Increases global contrast
 - Recalculates intensity using normalization of cumulative distribution function

Extra 9b: Histogram Equalization



Figure 1: Original



Figure 2: Equalized

Extra 9b: Histogram Equalization

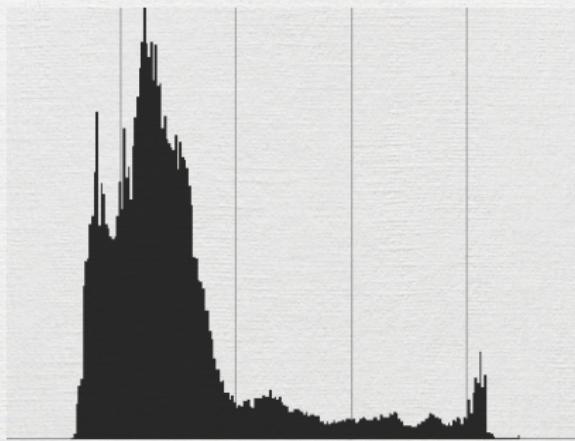


Figure 3: Original

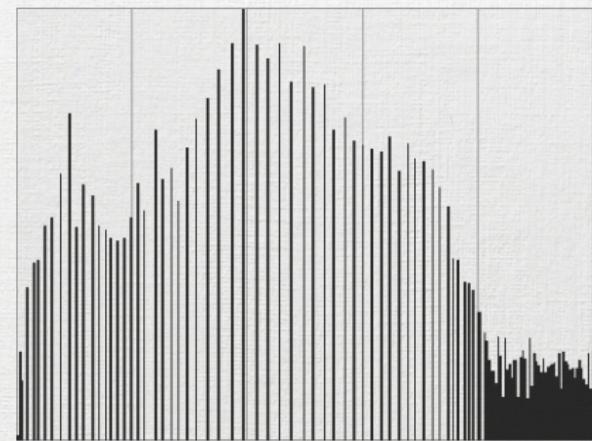


Figure 4: Equalized

Extra 9b: Histogram Equalization

- Calculate histogram `histo[]` (LW9a, GATHER + REDUCE)
- Let n be number of total pixels in the image
- Calculate probability of given intensity j (MAP)

$$p_j = \frac{histo_j}{n}, \forall j \in [0..255]$$

Extra 9b: Histogram Equalization

- Cumulative distribution function (CDF) c is calculated as ²

$$c_i = \sum_{j=0}^i p_j$$

- Linearly scale $c_i \in [0..1]$ to $h_i \in [0..255]$, $\forall i \in [0..255]$ (MAP)
- Original intensity i is transformed to h_i (MAP)
- We should have histogram equalized as now.

² c_i in this case should be calculated using parallel SCAN, but you haven't learnt about it yet. Let's do this step in sequential fashion.

Final Labwork: Fine-art transformation

- Implement Kuwahara filter, both with- and without- shared memory
- Write a report (in L^AT_EX)
 - Name it « Report.10.kuwahara.tex »
 - Explain how you implement the labworks
 - Explain and measure speedup
 - Without-shared memory vs CPU
 - With-shared memory vs without-shared memory
 - Other optimizations? Bank conflict? Coalesced access?
- Push the report and your code to your forked repository

Final Labwork: Fine-art transformation

- Kuwahara filter [[wikipedia](#)]
 - Reduces noise
 - Keeps edge
 - Also produces oil effect
 - Requires a lot of computation!

Final Labwork: Fine-art transformation

- Parameter ω as window size
- Convert RGB to HSV (SCATTER)
- For each pixel $\Phi(i, j)$
 - Define use 4 windows $W^k, k \in [1..4]$ of size $(\omega + 1) \times (\omega + 1)$
 - $W_x^1 \in [i - \omega, i], W_y^1 \in [j - \omega, j]$
 - $W_x^2 \in [i, i + \omega], W_y^2 \in [j - \omega, j]$
 - $W_x^3 \in [i - \omega, i], W_y^3 \in [j, j + \omega]$
 - $W_x^4 \in [i, i + \omega], W_y^4 \in [j, j + \omega]$

Final Labwork: Fine-art transformation

a	a	a	a/b	b	b	b
a	a	a	a/b	b	b	b
a	a	a	a/b	b	b	b
a/c	a/c	a/c	x	b/d	b/d	b/d
c	c	c	c/d	d	d	d
c	c	c	c/d	d	d	d
c	c	c	c/d	d	d	d

Figure 5: Example $\omega = 3$

Final Labwork: Fine-art transformation

- Find $W_l, l \in [1..4]$ having lowest standard deviation of brightness.
 - Use V in HSV color space to calculate SD.
- Assign mean (R, G, B) value of this window $| W_l |_{RGB}$ as new color (REDUCE, MAP)

$$\Phi(i, j)_{RGB} = | W_l |_{RGB}$$

Good luck & Have fun

